

# Influence of residual stresses on the buckling capacity of axially loaded steel column

Author : Gabriele Falconi

Professor in charge : Prof. Dimitrios Lignos <sup>1</sup>

Assistant in charge: Andronikos Skiadopoulos

<sup>1</sup> Resilient Steel Structures Laboratory (RESSLab), EPFL

## OBJECTIVES

Conduct measurements of residual stress distributions

- Perform the sectioning method on five different cross-sections
- HEA160, HEM500, IPE120, IPE200, and IPE360

Evaluate how existing codes predict the buckling resistance of steel members

- SIA 263:2013 (Switzerland)
- EN 1993-1-1:2005 (Europe)
- AISC 360-2016 (United States)
- CSA S16:2019 (Canada)
- AJ LFRD:1985 (Japan)

Evaluate the buckling resistance of steel members through finite element analysis

- Eight different cross-sections
- HEA160, HEB500, HEM300, HEM500, IPE120, IPE200, IPE360, and IPE400
- Five different critical lengths [normalised slenderness selection  $\bar{\lambda}_k$  (0.44; 1.67)]
- Initial imperfection influence
- Residual stress influence
- Assessment of the buckling curves according to the Swiss and European approach

## MOTIVATION

Manufacturing processes

- Quality improvements
- Less impact on the performance of steel elements

Normative revision

- Buckling curves based on rather old studies
- SIA 263:2013 (Switzerland)
- EN 1993-1-1:2005 (Europe)

## INTRODUCTION TO RESIDUAL STRESSES

Residual stresses as a state of equilibrated stresses along the cross-section

- No change in geometry
- $\sum \sigma_{rt} + \sigma_{rc} = 0$

Residual stress occurs due to the manufacturing process

- Cold lamination / Hot-rolled lamination / Extrusion / Forging / Welding

Residual stress as a function of the temperature

- Profile core temperature / Cooling process / Welding flame temperature

Detection of residual stresses

- Non-destructive methods
- X-Ray / Neutron diffraction / Magnetic measurements
- Destructive method
- Sectioning method

## EXAMPLE OF FLEXURAL BUCKLING RESISTANCE DESIGN APPROACH

SIA 263:2013 (Switzerland)

Buckling resistance

$$N_{k,Rd} = \chi_k \cdot f_y \cdot A / \gamma_{M1}$$

Reduction factor

$$\chi_k = \frac{1}{\phi_k + \sqrt{\phi_k^2 - \bar{\lambda}_k^2}} \leq 1$$

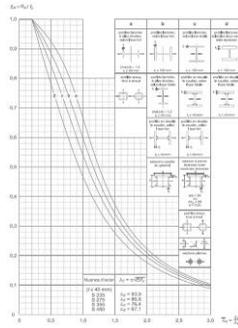
Slenderness ratio

$$\bar{\lambda}_k = \frac{\lambda_k}{\lambda_E} \quad \lambda_E = \pi \sqrt{\frac{E}{f_y}} \quad \lambda_k = L_k \sqrt{\frac{A}{I}}$$

$$\phi_k = 0.5 \left[ 1 + \alpha_k (\bar{\lambda}_k - 0.2) + \bar{\lambda}_k^2 \right]$$

Imperfection factors

Buckling curve	a	b	c	d
Imperfection factor $\alpha_k$	0.21	0.34	0.49	0.76



## ANALYTICAL DISTRIBUTIONS

Linear distributions

Galambos and Ketter (1958)

$$\sigma_t = \frac{\sigma_{rc}}{1 + \frac{d \cdot t_w}{b_f \cdot t_f} (1 - \frac{d}{t_f})} \text{ and } \sigma_c = 0.3 \cdot f_y$$

European Convention for Constructional Steelworks (1985)

$$\text{if } \frac{h}{b} \leq 1.2, \text{ then } \alpha = 0.5 \text{ else if } \frac{h}{b} > 1.2, \text{ then } \alpha = 0.3$$

Parabolic distributions

Young (1975)

$$\sigma_{c1} = 165 \left[ 1 - \frac{h_0 \cdot t_w}{2.4 \cdot B \cdot t_f} \right] \quad \sigma_{c2} = 100 \left[ 1.5 + \frac{h_0 \cdot t_w}{2.4 \cdot B \cdot t_f} \right]$$

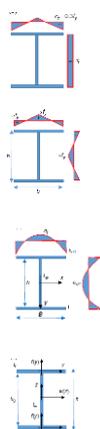
$$\sigma_c = 100 \left[ 0.7 + \frac{h_0 \cdot t_w}{2.0 \cdot B \cdot t_f} \right]$$

Bradford and Trahair (1985)

$$\sigma_f = \sigma_y \left[ a_1 + a_2 \left( \frac{z-y}{B} \right)^2 \right] \quad \sigma_w = \sigma_y \left[ a_3 + a_4 \left( \frac{z-z'}{B} \right)^2 + a_5 \left( \frac{z-z'}{B} \right)^3 \right]$$

Szalay and Papp (2005)

$$f(y) = c_f + a_f \cdot y^2 \quad w(z) = c_w + a_w \cdot z^2$$



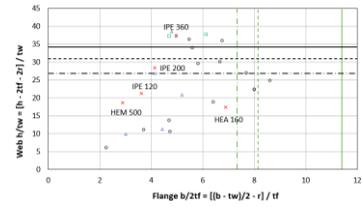
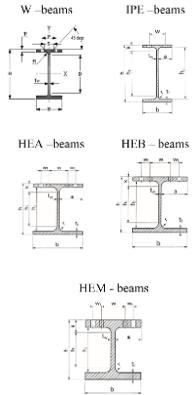
## STUDIES ON MESAUREMENTS AND PROFILE SELECTION

Investigations on residual stresses available in the literature

- E. Odar, F. Nishino and L. Tall (1965)
- L. Tall, T. V. Galambos and R.L. Ketter (1964)
- R. Trambly and C. P. Lamarche (2011)
- A. de Castro e Sousa and D. Lignos (2017)
- R.C. Spoorenberg, H.H. Snijder and J.C.D. Hoendekamp (2009)
- A. W. Huber (1956)
- N. Alpsten (1968)
- Y. Fujita, D. K. Feder and G. C. Lee (1955)

Additional profiles in analysis

- HEA160, HEM500, IPE120, IPE200, and IPE360



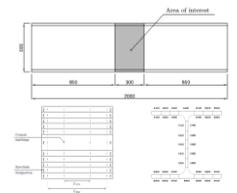
## THE SECTIONING METHOD

Rupture of the equilibrium of residual stresses by mechanical process

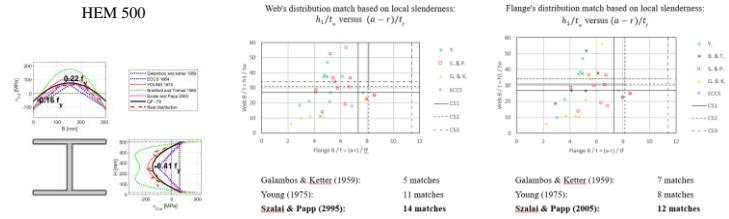
- Sectioning method

Material relaxation

- Measurement of length's differences
- Reconstruction of the stress state



## MESAUREMENTS OF RESIDUAL STRESSES



## CONTINUUM FINITE ELEMENT ANALYSIS (CFEA)

Model validation test reference

- "Seismically induced cyclic buckling of steel columns including residual-stress and strain-rate effects", C. P. Lamarche, R. Tremblay, 2011.

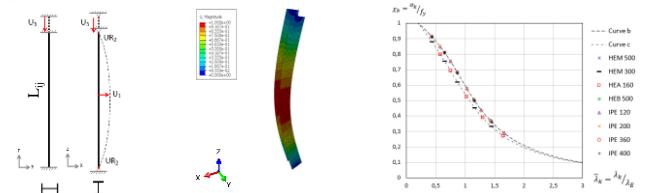
Material properties reference

- "On the inverse problem of classic nonlinear plasticity model", A. de Castro e Sousa, D. Lignos, 2018.

Generalized imperfection curves reference

- "Stability criteria for tubular-sections steel arches", 2019 NTUA Athens PHD Thesis, I. D. Thanasoulas, and C. J. Gantes.

Modelling assumptions



Results

- Design specifications comparison
- U.S. code (AISC 360-2016) – 27 best matches over 40 analysis
- Imperfection effect on the axial load capacity
- Resistance reduction up to 10% comparing e=L/1000 and e=L/3000
- Residual stress effect on the axial load capacity
- For  $\bar{\lambda}_k$  [0.65; 1.20] – Resistance reduction up to 22%
- For  $\bar{\lambda}_k$  ~ [1.50] – Global instability dominate the failure mode
- For  $\bar{\lambda}_k$  ~ [0.50] – Local buckling occurs
- Generalized imperfection curves
- Updated imperfection factors -  $\alpha_f$  from 0.34 to 0.17 and  $\alpha_c$  from 0.49 to 0.20

