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Capillary flow in UHPFRC with synthetic fibers, under high tensile stresses

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ABSTRACT

A novel Ultra High-Performance Fiber Reinforced Concrete (UHPFRC) mix with synthetic fibers and a low clinker matrix, henceforth referred to as *PE-UHPFRC*, has been developed for structural applications. It exhibits a high tensile elastic limit above 7 MPa, a tensile strength of more than 10 MPa, and a very high tensile hardening domain of above 3.5%. In order to effectively use this material, its protective properties have been investigated on the basis of the effect of tensile deformation and subsequent cracking on water transport properties, for a wide range of tensile strain. A special setup was developed to measure the capillary absorption of liquids while the specimen is under tension. The results show a considerable reduction in capillary absorption in case of PE-UHPFRC compared with Strain Hardening Cement-based Composites (SHCC). Moreover, the results highlight the considerable effect of the onset of cracking on capillary absorption.

1. Introduction

The ever-increasing demand of society for the build environments on one hand and the limited material resources, on the other hand, have promoted the implementation of high and ultra-high-performance materials towards sustainability during the last few decades. Meanwhile, UHPFRC has successfully gained the ground and has proved its potential to be one of the solutions to contain the explosion of the costs (economy and environment) along with its numerous applications [1-3]. Continuing this trend, PE-UHPFRC is developed with 75% reduced environmental impact compared to conventional UHPFRC mixes by replacing the steel fibers with Ultra High Molecular Weight Polyethylene (UHMW-PE) ones and replacing 50% of the clinker with limestone fillers [4]. The high tensile elastic limit above 7 MPa, tensile strength of more than 10 MPa, and tensile deformation capacity of more than 3.5% make the newly developed UHPFRC well adapted for structural applications. In order to effectively use this material, its protective properties need to be investigated on the basis of the effect of tensile deformation and subsequent cracking on water transport properties and accordingly on the durability of the material.

Deterioration mechanisms in cementitious materials are principally caused by insufficient protection followed by ingress of catalysts like water and aggressive agents in the material. Sorptivity and permeability are used as a measure for liquid transport properties and thereupon for the durability of cementitious materials. Permeability relates the movement of moisture through a saturated porous medium under a

pressure gradient. Consequently, it is not entirely representative as structures made from cementitious materials are rarely saturated and exposed to strong pressure gradients in the building environment (excluding underground and offshore structures). Hence, sorptivity is a more realistic property to describe the liquid transport and durability of cementitious materials in structural applications were capillary flow prevails. There are two general approaches to model and analysis the sorptivity of cementitious materials in literature, which both yield a linear relationship between capillary absorption and the square root of time. The first approach is based on an extension of Darcy's law to unsaturated porous media [5] and the second approach is based on the Lucas-Washburn equation [6,7], which describes the dynamic flow equation of liquids in a capillary tube. The latter approach is more employed to describe the capillary absorption of cracked cementitious materials [8–10] in which the sorptivity corresponds to the square root of crack width. Furthermore, Zaccardi et al. [11] reported a better correlation between the water capillary absorption, and the fourth root of time for normal concretes with ordinary Portland cement and pozzolanic Portland cement.

Different measurements for evaluating the transport properties, such as capillary absorption, gas penetration, and liquid penetration were carried out on undamaged UHPFRC specimens [12-18], which all show a considerable improvement compared to ordinary and high strength concretes. Roux et al. [18] showed that the capillary absorption of UHPFRC is over ten times less than that of conventional concretes. Furthermore, they reported that the air permeability and chloride

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diffusion coefficient of UHPFRC are at least two orders of magnitude less than that of C30 and C80 concretes. Tam et al. [16] found that the water permeability coefficient of UHPFRC is lower than that of normal concrete by one or two orders of magnitude. The resistance of UHPFRC to the penetration of chloride ions was investigated by many researchers [3,14,18] and it was shown that UHPFRC has a much higher resistance to penetration of chloride ions than ordinary concretes and that the depth affected from the surface of exposed areas is remarkably lower in UHPFRC. Furthermore, numerous studies have confirmed the durability of structures built with UHPFRC after several years of exposure to severe conditions [19–23]. These features are attributed to the homogenous and highly dense microstructure of UHPFRC.

At service state, structural elements experience different levels of mechanical loading under both autogenous (eigenstresses) and exogenous actions (climate conditions, live loads, deadweight, accidental actions, fire, etc.), well documented in the literature [24-26]. However, only a few notable studies were carried out on the effects of damage on the transport properties of UHPFRC [24-30]. Wang et al. [26] studied the influence of imposed compressive stresses on capillary absorption of UHPFRC and found that the absorbed water mass increased by a factor of two when the specimens were loaded up to 50% of their compressive strength. The effect of tensile stresses on capillary absorption was investigated by Wittmann et al. [24] and it was shown that the capillary absorption is significantly increased if the material is subjected to tensile stresses higher than 50% of its tensile strength. Accordingly, Wang et al. [25] reported that the sorptivity of UHPFRC increases by 30%, 45%, 77% and 95% for load levels of 50%, 60%, 70% and 80% of its splitting tensile strength, respectively.

ECC (Engineered Cementitious Composite) [31], SHCC [32] and HSHDC (High Strength, High-Ductility Concrete) [33] are classes of synthetic fiber-reinforced cementitious composites with high tensile deformation capacity. Although from a mechanical properties point of view, HSHDC is the closest to PE-UHPFRC, to the best of authors' knowledge, no extensive research has been reported in the open literature on transport properties of this material. However, the durability of ECC and SHCC, which are designed to limit the ingress of potentially deleterious substances by controlling cracks width, were investigated in terms of transport properties, as a function of different crack width and strain levels by several researchers [34-43]. The results show that the water permeability under pressure is very much linked to the crack features and cracking patterns. Regardless of the material type (SHCC, normal concrete and UHPFRC), the permeability to liquids under pressure starts increasing at a much faster rate with increasing crack width after 0.05 to 0.1 mm [30,40,41]. However, the capillary water absorption in SHCC specimens was found to increase drastically by increasing the strain in the specimens even before a crack opening of 0.1 mm [39]. Investigations by means of neutron radiography showed that preexisting microcracks subjected to capillary absorption become waterfilled only after a few minutes [44]. Furthermore, increasing strains from 0 to 0.5% results in almost a 72% higher water capillary absorption [42]. Although the crack width plays an important role on the capillary absorption of cementitious materials, its effects have been underestimated in the aforementioned studies as the capillary absorption was determined after unloading the specimens.

In this study, an original test setup was developed in order to measure the capillary absorption of materials under tensile loading. The water sorptivity of tensile specimens made from PE-UHPFRC was investigated over a wide range of tensile deformation with the help of the developed setup. Afterwards, the specimens were unloaded and the capillary absorption of the same specimens was determined in accordance with EN13057:2002 standard [45], in order to compare the sorptivity under load and after unloading. As the cracking behavior highly affects the capillary absorption, Digital Image Correlation (DIC) was used to analyze the crack characteristics including crack pattern and width and investigate their effect on sorptivity. Finally, the results were put into perspective with existing experimental data on related

Table 1Mix proportions of PE-UHPFRC (mix PE21).

Components	(kg/m^3)
Cement	508
Silica fume	118
Betocarb®-HP SL	170
Betoflow®-D	389
Quartz powder	223
Fine sand	525
Water	165
HRWRA	27
Ca(NO ₃) ₂	11
UHMW PE fibers (Dyneema® SK99)	19.6

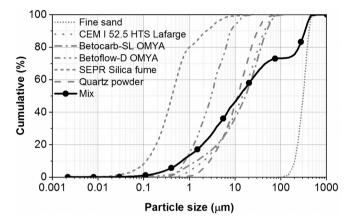


Fig. 1. PSD of the components and final mix.

materials.

2. Material design

A newly developed UHPFRC mix, named "PE-UHPFRC" (ref. mix PE21), was used for the present study. The Embodied Energy (EE) of this mix is reduced by 75% with respect to that of current UHPFRC mixes for structural applications, with steel fibers. In PE-UHPFRC mixes, the steel fibers are fully replaced by UHMW-PE ones and 50% volume of the clinker is replaced by limestone fillers. Considering that the optimization of packing density and low w/fines ratio are the keys for obtaining Ultra high-performance cementitious composites, a generalization of the Compaction-Interaction Packing Model (CIPM) model [46] was derived and applied to optimize the mixture design [4]. Six different powders including cement CEM I 52.5 HTS Lafarge, two types of limestone filler of different gradings: Betoflow D® and Betocarb SL® (OMYA), white silica fume from SEPR (BET = $14 \text{ m}^2/\text{g}$), quartz powder and fine quartz sand ($d_{50} = 0.250$ mm) were used in the mixes. Moreover, a modified Polycarboxylates-based HRWRA was used to maintain flowability and rheology of the mixture at the very low w/fines ratio of 0.146. The composition of the PE-UHPFRC mix is given in Table 1. Moreover, Fig. 1 shows the particle size distribution (PSD) of the powders used and of the mix. The packing density of the final mix was 0.81 based on the generalized CIPM, by using a compaction index of 9 for the calculations.

Table 2Geometry and mechanical properties of PE Fiber.

Fiber properties	Values
Diameter d _f (μm)	12
Length l _f (mm)	6
Nominal strength (MPa)	4100
Nominal Young's modulus (GPa)	155
Elongation at break (%)	3.5
Specific weight (kg/m³)	980

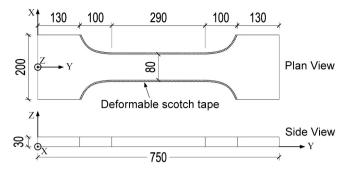


Fig. 2. Dumbbell specimen geometry (dimensions in mm).

 $\text{Ca}(\text{NO}_3)_2$ was employed in the form of a water-soluble compound in order to optimize the performance of the superplasticizer and reduce its dosage and thus the air content. At fresh state, the air content and the specific weight of the material were 4.5% and 2215 kg/m³, respectively. Furthermore, the flow was 48% after ASTM C1437 [47], with a final diameter after 25 blows of 150 mm.

The fibrous mix consisted of 2% vol. 6 mm long, chopped UHMW-PE fiber type SK 99 from DSM Dyneema®. The mechanical properties and the geometry of these PE fibers are given in Table 2.

3. Experimental procedure

3.1. Specimen design and preparation

An original dumbbell specimen was designed with a thickness of 30 mm representative of that found in numerous applications of UHPFRC, either cast-on-site for rehabilitation or in structural uses with thin precast ribbed members. The specimen had 290 mm length with a constant cross-section, with a width of 80 mm, on which three capillary chambers were installed (Figs. 2 and 5). The total length of the specimen was 750 mm. In order to limit as far as possible stress concentrations, Neuber's model [48] was applied to determine the geometry of the 100 mm long transition zone between the specimen's ends and its central part. Fig. 2 shows the corresponding specimen geometry.

The specimens were cast horizontally in the molds from one end to

the other, in a systematically repetitive procedure to obtain reproducible fiber orientation and distribution. The lower internal face of the molds was covered with a Controlled Permeability Formliner (CPF) - Zemdrain® sheet to avoid the water repellent effect of demolding oil. In order to avoid surfacing, the top surface of the specimen was covered immediately after pouring with a Zemdrain® sheet attached to a wood panel to guarantee a flat and uniform upper surface without air voids, after setting. Regarding the use of Zemdrain® sheets on the UHPFRC surfaces, it should be noted that according to [49], using these sheets had a negligible effect on the air permeability of concretes with a w/c ratio of 0.43. It can thus be assumed that their effect on the mechanical and transport properties of the UHPFRC skin are negligible. Moreover, the lateral internal faces of the molds along the shoulders were covered with 1 mm thick deformable tape to prevent eigenstresses and restrained shrinkage cracks at an early age. The specimens were kept sealed after casting for 2 days at room temperature of 20 \pm 5 °C. Thereupon demolding, the specimens were stored at room temperature of 20 \pm 5 $^{\circ}$ C under 95% RH. Before testing at 28 days, the specimens were washed with soap, to ensure removing of any fat with a water repellent effect. This was followed by a drying process at 50 °C up to a constant weight. Eventually, the specimens were stored in the laboratory at ambient conditions (20 °C under 50% RH) for at least 12 h.

3.2. Tensile test

In order to avoid as far as possible bending effects during the test, an optimized set-up was used with: (1) a stiff (4 columns) testing machine, (2) fixed/fixed support conditions for the specimen, and (3) a highly accurate alignment of the specimen thanks to a special procedure to link it directly to the machine without clamping. The dumbbell specimens were attached to the testing set-up by means of the "gluing without bonding" approach proposed by [50], and applied to dumbbell specimen by [51], Fig. 3. A steel shoe formed of plates with indented internal faces (c) on Fig. 3, was used as a form to cast resin indentations glued to the specimen, that helped transmit loads from the machine to the specimen by interlocking. In order to avoid adherence between the specimen and the indented metallic shoe, a demolding spray was applied on the internal indented faces of the later, before inserting the specimen coated with resin on its end in the shoe. This system guaranteed a uniform stress

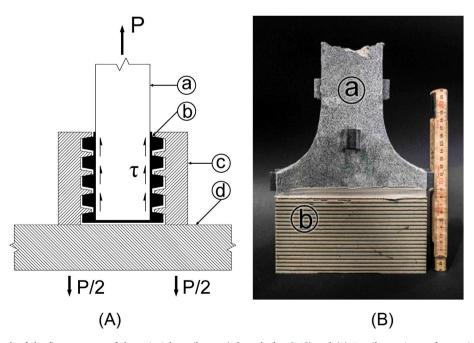


Fig. 3. (A) Schematic sketch of the fixture set-up of the uniaxial tensile test (adapted after [50]) and (B) Tensile specimen after testing, with (a) specimen, (b) hardened resin indentations glued to the specimen surface, (c) indented steel plate, and (d) base plate.

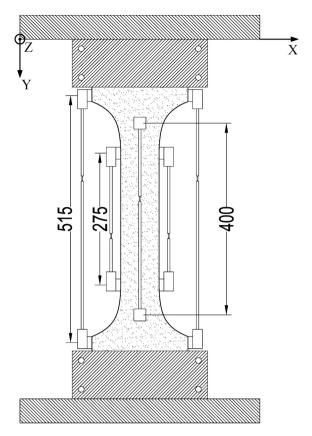


Fig. 4. Test setup and instrumentation of the tensile specimen (dimensions in mm).

transfer without lateral restraint of the specimen. The top and bottom indented steel shoes were tightly bolted to stiff steel plates, (d) on Fig. 3, bolted directly on the machine's heads without any hinge.

The uniaxial tensile tests were conducted with a universal AMSLER testing machine (capacity: 1000 kN). The test was controlled by the mean value of two LVDT fixed on the specimen with a gauge length of 515 mm, as shown in Fig. 4, with a closed-loop deformation rate of 0.003 mm/s. Two additional pairs of LVDT, set in two perpendicular planes, were used to determine the elongation of the specimen and check eccentricities under loading. The gauge lengths of the LVDT were 400 mm and 275 mm in XY and YZ planes, respectively.

3.3. Crack measurement system

A 3D Digital Image Correlation (DIC) system, was used in order to measure the surface deformations. The system consisted of two 29 MP SVCam-hr29050 cameras with Zeiss Distagon35 lenses, connected to a PC. The digital images were analyzed by the Vic-3D 8 software in order to determine the surface deformation. In order to make an identifiable pattern, first the cast upper surface of the specimen was painted in white and then black aerosol paint spray was used to create the speckle pattern. The measurement area was 350 mm \times 80 mm. The resolution of deformation measurement was 0.2 μm .

3.4. Capillary absorption test

An original setup was developed in order to measure capillary absorption while the specimen was loaded. The setup consisted of 3 cylindrical chambers with an internal diameter of 60 mm, which maintained the liquid in contact with the specimen surface. The chambers were made from Plexiglas that rested on an aluminum support. Two chambers (one for the specimen and the other one for the reference)

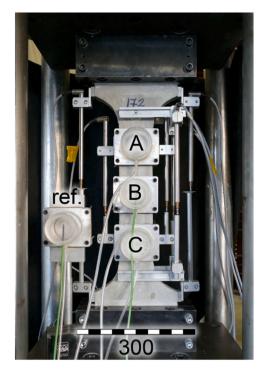


Fig. 5. Capillary absorption measurement setup with chambers A, B and C installed on the tensile specimen, and additional reference chamber for compensation of effect of temperature variations.

were equipped with thermocouples in order to have a live measurement of the liquid temperature during the test.

For the capillary measurements, three chambers were clamped on the constant cross-section of the specimens with the help of 4 threaded rods. A rubber gasket was placed between the specimen surface and the chamber's support in order to ensure the water tightness. Each chamber was then connected to a graduated glass pipette with a flexible plastic tube. A drop of oil was put over the water in the pipette to avoid evaporation and the liquid level in the pipettes corresponded to the level of the chambers to avoid hydrostatic pressure at the beginning of the test. The subsequent changes of the liquid level were then recorded using a non-contact optical measurement system based on a digital camera and real-time image processing. As a reference, one chamber was clamped on an aluminum plate and was placed close to the specimen in order to record the variation of the water level due to the effect of ambient condition such as temperature variations and evaporation. This variation was then subtracted from the water level of the other three chambers in order to have only the effect of capillary absorption. The installation of the capillary absorption setup is presented in Fig. 5.

After the capillary absorption test under tension was completed, the damaged dumbbell specimens were unloaded, and cores were extracted for the capillary absorption tests based on EN13057:2002 standard [45]. Three cylinders were cut throughout the full depth (30 mm) of the tensile specimen with water jet, at the exact locations which were in contact with the chambers during the capillary absorption measurement under tension, to be able to compare the results, Fig. 6 (a). Afterwards, the cylinders were oven dried until constant weight, at 50 °C. In order to ensure one-dimensional liquid transport, the side faces of the cylinders were sealed with paraffin and thereafter, the specimen was kept in the laboratory ambient conditions (20 °C) for at least 12 h before being placed in the standard capillary absorption setup. Throughout the absorption tests, the immersion depth was kept constant at 2 mm. The standard capillary absorption setup is schematically shown in Fig. 6 (b).

The capillary absorption coefficient was calculated based on Eq. 1, from the slope of the absorption versus square root of time in both cracked and uncracked states.

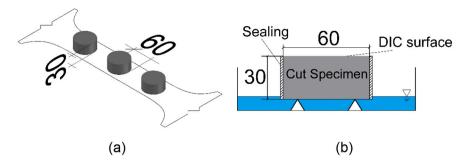


Fig. 6. Dimensions and location of the cores extracted from the dumbbell specimen (a) and, a schematic sketch of standard capillary absorption setup (b) (dimensions in mm).

Table 3 Overview of the performed tests.

Specimen no.	Loaded until	Capillary absorption under tension	Capillary absorption after unloading	
1	Ultimate strain	-	-	Tensile prop. & crack char.
2	Ultimate strain	-	-	crack char.
3	Ultimate strain	-	-	
4	0.015%	3× chambers	_	Serviceability
5	0.03%	3× chambers	_	domain
6	0.05%	$3\times$ chambers	3× cylinders	
7	0.05%	$3\times$ chambers	_	
8	0.1%	3× chambers	3× cylinders	
9	0.15%	3× chambers	$3 \times$ cylinders	
10	0.2%	3× chambers	$3 \times$ cylinders	
11	1%	3× chambers	$3 \times$ cylinders	Large
12	2%	$3\times$ chambers	$3\times$ cylinders	deformation

$$i = S.t^{0.5} \tag{1}$$

where i is the cumulative absorption, t is time, and S is a constant referred as the sorptivity (capillary absorption coefficient).

It should be born in mind that original UHPFRC made with a majority of reactive powders have a very low degree of hydration, due to their very low w/b ratio [52,53]. Thus, delayed hydration of the unhydrated binders when the material is in contact with water during permeability tests over several weeks may influence results, and require the use of different liquids not reacting with cement [27]. However, this effect was neglected in this study as the exposure time to water was short

and also the amount of unhydrated binders was significantly lower for the investigated PE-UHPFRC compared with conventional mixes, because of the replacement of 50% of the clinker by limestone filler. The maximum degree of hydration for PE-UHPFRC was 52% and 60%, after Waller [54] and Jensen [55] models, respectively.

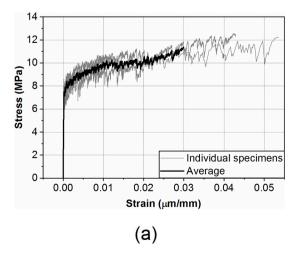
3.5. Overview of performed tests

Table 3 gives an overview of all the performed tests. Three uniaxial tensile tests until the end of hardening were performed in order to characterize the tensile behavior of the material. Capillary absorption tests were carried out on the specimens for a wide range of tensile strain levels. The investigated strain levels are 0.015%, 0.03%, 0.05%, 0.1%, 0.15%, 0.2%, 1% and 2%. First, the specimens were loaded to the defined strain levels, measuring the strain with the help of two LVDTs with the gauge length of 515 mm (Fig. 4). Meanwhile, the crack characteristics were recorded by means of DIC. Afterward, the chambers were installed on the surface of the specimens and the capillary absorption measurement started. Considering the effect of saturation conditions on the capillary absorption, a separate specimen was tested for each strain level. Repetition was done for the strain level of 0.05% to characterize the variability of the obtained results.

4. Results and discussion

4.1. Tensile response and evolution of damage under tension

The uniaxial tensile test results of all the tested specimens are shown in Fig. 7. The x-axis shows the average tensile strain computed from the extensions of two pilot LVDT that controlled the deformation with the gage length of 515 mm (setup shown in Fig. 4).



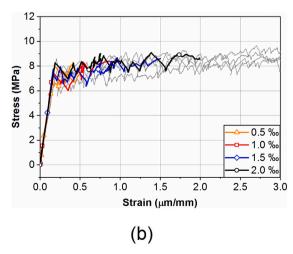


Fig. 7. Uniaxial tensile stress-strain response of the tested PE-UHPFRC specimens (a) zoom until 0.3% strain level (b).

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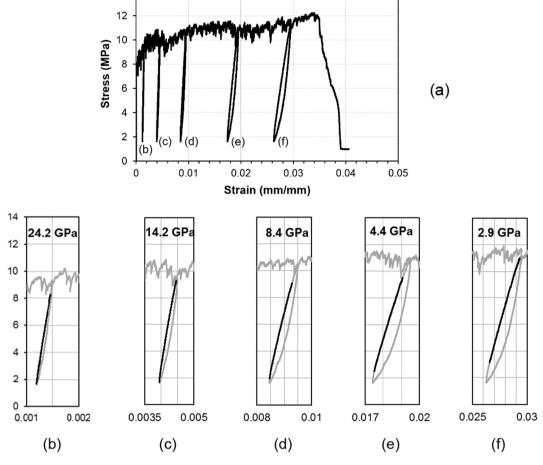


Fig. 8. Unloading-loading cycles and apparent E modulus of a tensile specimen at different strain levels.

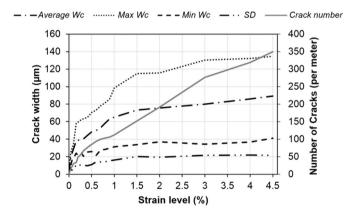


Fig. 9. Crack number, and average, maximum, minimum and standard deviation of the crack width under tension of specimen No. 2.

The specimens had a strain-hardening behavior and numerous multiple cracks developed gradually. As it is shown in Fig. 7, the elastic limit (first crack strength) was above 7 MPa. The average elastic modulus of the material in tension was 43 GPa, which was computed from the slope of the average straight line through the stress-strain data points of the specimen. Furthermore, it should be noted that compared to other results from the literature [33], the stress fluctuation in the hardening zone was much lower. Fig. 7 highlights highly reproducible tensile test results which confirm the robustness of the material and the effectiveness of the testing setup.

The evolution of damage under tension is an important property, which can be characterized by determining the apparent E modulus at different tensile strains by performing unloading-loading cycles. Fig. 8 shows the unloading-loading cycles and the apparent E modulus of a tensile specimen at strain levels of 0.15, 0.4, 1, 2 and 3%.

4.2. Crack characteristics

The crack characteristics were analyzed up to the strain level of 4.5%. Considering the yield strain of approximately 0.2% for conventional steel reinforcement in structural members, 4.5% strain will never be reached under service loads in RC structures. However, investigating higher strains is still important to understand the full picture of the evolution of the cracks and of the associated capillary absorption. Fig. 9 shows the crack numbers, and average, maximum, minimum and standard deviation of the crack width (w_c) for a uniaxial tensile test. The specimen exhibited a multiple cracking behavior and the average crack widths did not exceed 0.1 mm even up to a very high strain level of 4.5%.

Fig. 10 shows the DIC images of the tensile specimen No. 2 at strain levels of 0.1, 0.2, 1, 2, 3 and 4% along with the crack analysis. The horizontal lines indicate the crack location and the dots show the corresponding crack width. The gauge length of the strain $\epsilon_{yy},$ which is represented by the colored contour plot, was 20 pixels, which was 1.43 mm in this study.

Fig. 11 represents the distribution of the crack width at the strain levels of 1, 2, 3 and 4%. For the strain levels of 1 and 2%, a lognormal distribution fits well on the results, as suggested in the literature for ECC and SHCC materials [37,38,56]. However, for the higher strain levels of

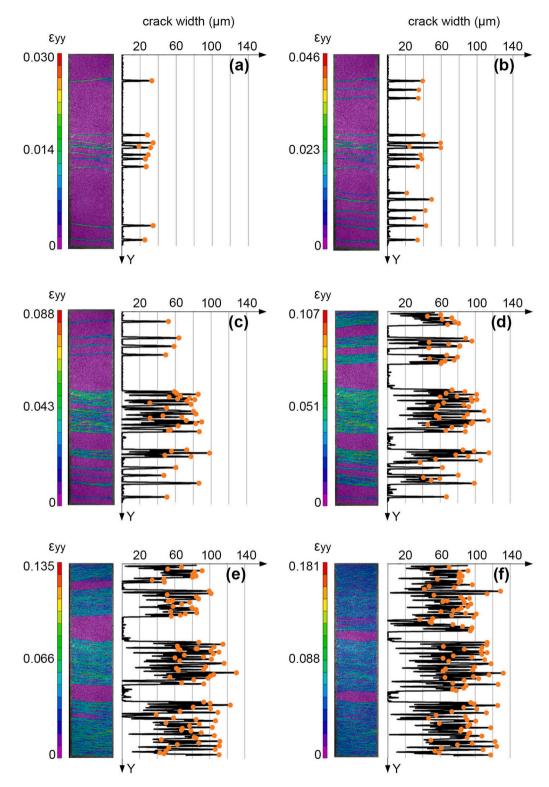


Fig. 10. DIC images of the tensile specimen No.2 at different strain levels along with the crack analysis. (a) 0.1%, (b) 0.2%, (c) 1%, (d) 2%, (e) 3%, and (f) 4%.

3 and 4%, the distribution of the crack width was closer to a normal distribution, Fig. 11 (b).

Fig. 12 illustrates the crack width after unloading for a strain level of 4%. As it is shown, the maximum crack width after unloading decreased significantly and reached below 0.05~mm.

4.3. Capillary absorption test under tension

Fig. 13 shows the average water capillary absorption under tension from the three chambers, for the strain level of 0.015 to 0.2%. Considering that the elastic limit of the material was around 0.02%, the strain level of 0.015% was in the elastic domain and the specimen was still uncracked. The capillary absorption coefficient for this strain level was in the extremely low range of 3 to 4 g/m $^2\sqrt{h}$ that confirms the very

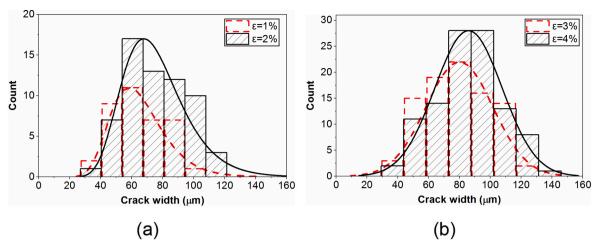


Fig. 11. Crack width distribution: (a) for 1 and 2% strain levels - lognormal distribution, and (b) for 3 and 4% strain levels - normal distribution.

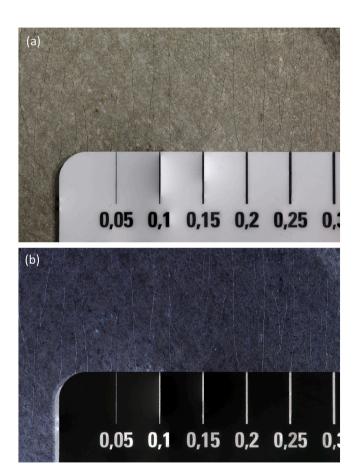


Fig. 12. Crack width after unloading for a strain level of 4%, (a) normal and (b) inverted.

dense microstructure of the material. The strain level of 0.03% was just after the elastic limit at which there was only one crack on the specimen. Accordingly, only the chamber that was on the cracked area was showing higher values and the capillary absorption from the two other chambers remained close to 4 g/m $^2\sqrt{h}$.

Fig. 14 represents the crack patterns with respect to the location of the chambers as well as the crack widths for the strain levels of 0.05, 0.1, 0.15 and 0.2%. In this figure, the positions of the cracks are outlined by dashed lines and the circles show the position of the chambers on the specimens. At the strain level of 0.05%, two cracks with widths of 50.2

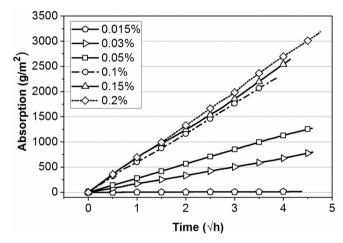


Fig. 13. Average water capillary absorption under tension, from three chambers for the strain levels of 0.015 to 0.2%.

μm and 33.6 μm along a length of 29.7 mm and 38.1 mm, respectively, were present under the top chamber (A). One crack with a width of 38.8 μm along a length of 57.6 mm was present under the middle chamber (B). Finally, one crack with a width of 44 μm along a length of 58.7 mm was present under the bottom chamber (C). The average capillary absorption coefficient at this strain level was 293 and 313 g/m $^2 \sqrt{h}$ for the first and the repeated specimen, respectively.

At the strain level of 0.1%, two cracks were present under chamber A, while there was one crack each within the area of both the other chambers. According to Table 4 and Fig. 14, the widest crack with a width of 70.7 μm highly influenced the capillary absorption in the top chamber while the other two chambers exhibited similar capillary absorption with a similar crack pattern.

For the strain level of 0.15%, nine cracks with an average width of 34 μm located under chamber A, and three cracks with an average width of 85 μm under chamber B, had a similar effect on capillary absorption. The capillary absorption of the bottom chamber (C), which did not experience any crack in its area, remained close to 4 g/m² \sqrt{h} .

At the strain level of 0.2%, more cracks developed on the top and bottom part of the specimen compared to the center. Six cracks were found under chamber A. However, the cracks were situated close to the end of the chamber and therefore their lengths which were in direct contact with water, were shorter compared to that for the other two chambers. Two cracks with widths of 40.1 μm and 46.4 μm were present under chamber C. Four cracks with the width range of 50 to 100 μm were

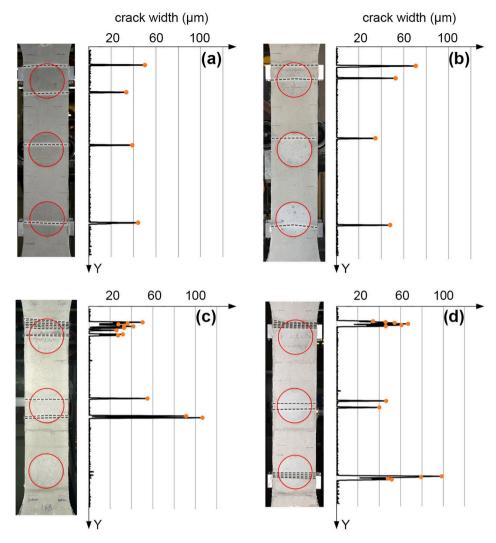


Fig. 14. Crack positions and the corresponding crack width for the specimens loaded up to strain levels of (a) 0.05%, (b) 0.1%, (c) 0.15% and (d) 0.2%.

Table 4 Capillary absorption coefficients $(g/m^2\sqrt{h})$ under tension, from each chamber and the average values for strain levels of 0.03 to 2%.

Strain level	0.03%	0.05%	0.05%	0.1%	0.15%	0.2%	1%	2%
Chamber A	4	315	348	976	935	651	1612	4341
Chamber B	502	314	300	390	932	689	1915	2682
Chamber C	4	250	291	397	4	717	1659	3724
Average	170	293	313	588	624	686	1729	3582

present in the middle of the bottom chamber and resulted in a higher capillary absorption for this chamber.

Fig. 15 outlines the average water capillary absorption of the specimen from three chambers against the square root of hour, for the strain levels of 1 and 2%, under tensile loading. At 1% strain level, the specimen experienced 38 cracks along a length of 354.5 mm, which represents a crack density of 107 cracks per meter. The average of the crack width was 68.5 μm with a standard deviation of 17.4. The capillary absorption coefficient of the specimen varied from 1600 to 1900 g/ $m^2 \sqrt{h}$ for the three chambers.

The crack density at the 2% strain level was 236 cracks per meter with the average crack width of $68.2~\mu m$ and a standard deviation of 18.7. With respect to the crack characteristics at 1% strain level, the number of cracks increased by a factor of two, while the average crack width and standard deviation remained in a similar range. The average capillary absorption coefficient for the three chambers at a 2% strain

level was 3582 g/m² \sqrt{h} . This is a very high value comparable with the capillary absorption coefficient of red brick that is approximately 4000 g/m² \sqrt{h} .

The capillary absorption coefficient was calculated for each individual chamber and is shown in Table 4 for the strain levels of 0.03 to 2%. The variation of the capillary absorption from different chambers at the strain levels below 0.2% is the result of a limited number of cracks and consequently non-uniform crack patterns at those strain levels. At the strain level of 0.03%, there was only one crack on the specimen under the chamber B. Similarly, as it is shown in Fig. 14, there was no crack under the chamber C at the strain level of 0.15%.

In order to highlight the effect of cracks on capillary absorption, Fig. 16 shows the capillary absorption as a function of crack area for the specimen tested at 0.05, 0.1, 0.15 and 0.2% strain level. In this figure, each point corresponds to one chamber and the crack area was calculated by the sum of the crack widths times crack lengths under the

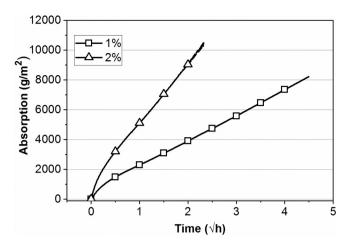


Fig. 15. Average of water capillary absorption under tension, from three chambers for the strain levels of 1 and 2%.

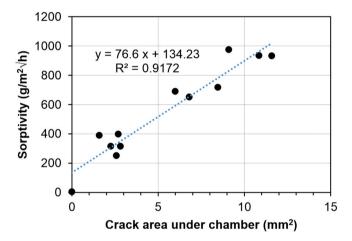


Fig. 16. Capillary absorption as a function of the crack area until the strain level of 0.2%.

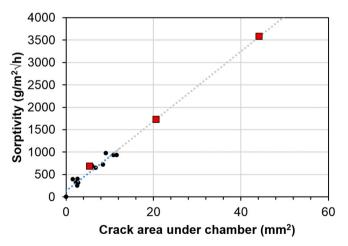


Fig. 17. Validation of the averaging method.

chamber. The results showed a linear relation relationship between the capillary absorption and the crack area.

In order to validate the averaging method used for reporting the capillary absorption at different strain levels, the average capillary absorption at strain levels of 0.2, 1, and 2% from Table 4 were plotted in

Fig. 17 versus the crack area calculated based on Fig. 9 and were compared with the linear relationship calculated in Fig. 16. The results fitted well on the linear relationship which confirmed both the validity of the averaging method and the crack information provided in Fig. 9.

4.4. Capillary absorption test after unloading

Specimen for capillary absorption tests after unloading were cored out of the dumbbell specimens for strain levels of 0.05%, 0.1%, 0.15%, 0.2%, 1% and 2%. Fig. 18 shows the average absorption of three cores, which were taken from each specimen after unloading on the same locations as that of the respective chambers A, B, C. The capillary absorption increased gradually with increasing strain levels. Although there was a linear correlation between capillary absorption and the square root of time for the lower strain levels (0.05 and 0.1%), the relation deviated from linearity at the higher strain levels. This can be explained by the contrary effect of gravity on the capillary rise in the wider cracks which takes place for the configuration of the test after EN13057:2002 [45] (soaking from bottom face).

Table 5 presents the capillary absorption coefficient of the specimens that were tested after unloading (individual results and average), for the investigated strain levels.

4.5. Discussion

Fig. 19 compares the capillary absorption of PE-UHPFRC with that of SHCC under various strain levels, taken from Mechtcherine et al. [36] and Wittmann et al. [43]. In this figure, the capillary absorption coefficient of PE-UHPFRC is the average of three values. In all the cases, the specimen is damaged under tension and the capillary absorption test is performed on the cores from the tensile specimen after unloading.

It can be noticed from Fig. 19 that the water capillary absorption of PE-UHPFRC is at least one order of magnitude lower than that of SHCC. This highlights the fact that although crack width limitation criteria are a necessary condition for durability, the density of the microstructure plays an equally important role on transport properties and thereupon on the durability of the material. Moreover, as it can be seen in this figure, even after experiencing the strain level of 2%, after unloading, the absorption coefficient of PE-UHPFRC is lower than that of undamaged normal concrete, which is in the range of 300 g/m $^2\sqrt{h}$.

The influence of imposed tensile stresses on capillary absorption of UHPFRC with steel fibers under tensile loading has been investigated by Wittmann et al. [24]. Tensile test results for the same material are presented in [57]. On this basis and considering a typical range of strain levels corresponding to elastic limits of PE-UHPFRC from 0.015 to 0.02%, Fig. 20 shows a sudden increase in capillary absorption coefficients after the elastic limit. A similar trend was observed for the PE-UHPFRC.

Moreover, the capillary absorption coefficient of steel fiber UHPFRC decreases by approximately 35% after unloading while according to Fig. 21, the capillary absorption of PE-UHPFRC decreases at least 10 times after unloading. This can be explained by different crack closure behaviors of these two materials after unloading. The stiffness of steel fibers hinders the closure of cracks, while synthetic fiber can hardly oppose to crack closure after unloading.

The durability related requirements for the Serviceability Limit State (SLS) depend on both material properties and the expected service life of the structure. Considering that the expected service life for UHPFRC applications is the full service life of the structure without any further rehabilitation, the UHPFRC layer should remain impermeable during the whole remaining service life of the structure after rehabilitation, to fulfill the SLS criteria. The French standard on UHPFRC [58] followed the normal and fiber-reinforced concrete codes [59] and recommended limitations on the maximum crack width for the durability related SLS. However, this approach is questionable according to the results of this study and other investigations reported in the literature [24,60]. As

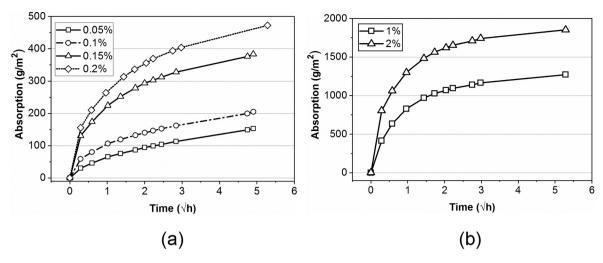


Fig. 18. Average of water capillary absorption test results from three cores, for the strain levels of (a) 0.05 to 0.2%, and (b) 1 and 2%, after unloading.

Table 5 Capillary absorption coefficients (g/m $^2\sqrt{h}$) for tests after unloading, from each core and the average values for strain level of 0.05 to 2%.

Strain level	0.05%	0.1%	0.15%	0.2%	1%	2%
Core A	25	46	87	57	203	142
Core B	24	18	53	48	186	211
Core C	25	22	5	77	75	224
Average	25	29	48	61	155	192

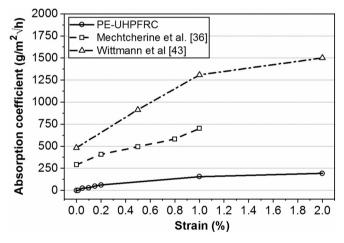


Fig. 19. Comparison between capillary absorption coefficient of PE-UHPFRC, and SHCC at different strain level after unloading.

such, in order to provide proper protective function throughout the entire lifetime of the structure, the PE-UHPFRC layer should stay uncracked. Thus, the sum of the tensile stresses in a PE-UHPFRC layer from internal and external action effects should remain below the tensile elastic limit of the material at SLS, from a purely local, deterministic point of view. However, further investigations should be carried out to generalize these findings to the determination of Serviceability Limit States for Strain Hardening UHPFRC in structural members considering the deterioration mechanisms followed by the ingress of liquids through microcracks in UHPFRC, with or without rebar.

5. Conclusions

The effect of the strain level on the capillary absorption of water in

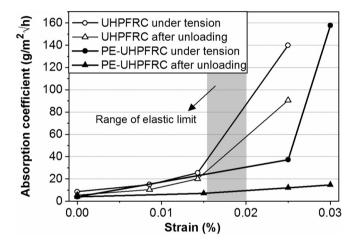


Fig. 20. Capillary absorption of UHPFRC with steel fibers and PE-UHPFRC versus strain level.

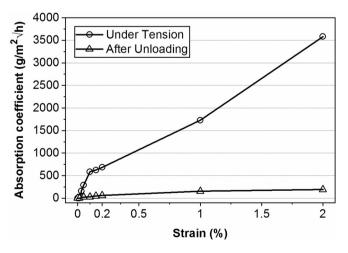


Fig. 21. Average capillary absorption coefficient of the PE-UHPFRC versus strain level.

PE-UHPFRC was investigated in two ways: (I) under tension, using an original testing setup, and (II) after unloading, based on standards. According to the results,

- The cracking behavior of PE-UHPFRC was similar to that of other cementitious materials with high deformation capacity (ECC and SHCC), up to a strain level of 2%, and the cracks width similarly followed a lognormal distribution. The average crack width remained below 0.1 mm throughout the tensile behavior. However, for higher strain levels (3 and 4%), the crack width distribution changed towards a normal distribution.
- The capillary absorption of PE-UHPFRC after unloading was at least ten times less than that of SHCC, which is a comparable cementitious materials in terms of deformation capacity, at all the studied strain levels.
- There was a sudden significant increase in capillary absorption of UHPFRC (including literature) after the elastic limit under tensile loading.
- The capillary absorption of damaged PE-UHPFRC after unloading increased gradually with the strain level, and remained below 60.9 ${\rm g/m^2}\sqrt{\rm h}$ even after experiencing a strain level of 0.2% before unloading.
- There was a considerable difference of approximately one order of magnitude in the rate of liquid ingress, when comparing the capillary absorption of same PE-UHPFRC samples, under tension and after unloading. This highlights the necessity of developing more realistic test methods in order to define the durability properties and serviceability limit state of cementitious materials with high deformation capacity.
- Although crack width limitation is a necessary condition for durability, the density of the microstructure of the material plays an equally important role on transport properties and thereupon on its durability and protective properties.
- Fixing threshold values of crack width for durability must be done considering the relevant transport mechanisms.

CRediT authorship contribution statement

- A. Hajiesmaeili1, E. Denarié2.
- 1 corresponding author, conducted all the experiments presented in the paper along with the writing of the full article.
 - 2 thesis supervisor.

Declaration of competing interest

The authors declare no conflict of interest.

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